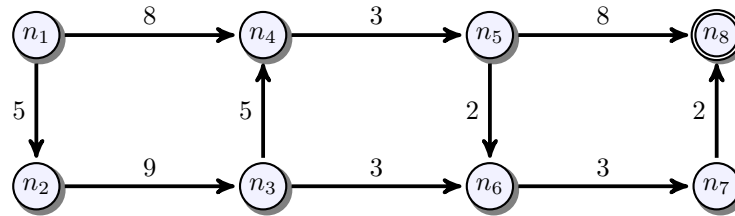




Student Name: \_\_\_\_\_

HW#4 CVL851: Special Topics in Transportation, Spring 2023

**Problem 1** (20 Points) The final state in the figure is  $n_8$ . Using Bellman's principle for Dynamic Programming, find the value function for every state, and using that find the shortest path sequentially from  $n_1$  to  $n_8$ , and also from  $n_3$  to  $n_8$ .



**Problem 2** (20 Points)

1. Given the optimization problem

$$\text{minimize } \int_{t_0}^{t_f} f(t, x(t), \dot{x}(t)) dt, \quad x(t_0) = x_0, \quad x(t_f) = x_f$$

derive the Euler Lagrange condition to be solved.

2. Solve the problem

$$\text{minimize } \int_0^{\pi/2} (\dot{x}^2(t) - x^2(t)) dt, \quad x(0) = 0, \quad x(\pi/2) = 1$$

**Problem 3** (50 Points)

1. What is the probability of getting three sixes in three rolls of a dice?
2. A subway train made up of  $n$  cars is boarded by  $r$  passengers ( $r \leq n$ ), each entering a car completely at random. What is the probability of the passengers all ending up in different cars?
3. A batch of 100 manufactured items is checked by an inspector, who examines 10 items selected at random. If none of the 10 items is defective, he accepts the whole batch. Otherwise, the batch is subjected to further inspection. What is the probability that a batch containing 10 defective items will be accepted?
4. What is the probability that two playing cards picked at random from a full deck are both aces?
5. What is the probability that each of four bridge players holds an ace?



Student Name: \_\_\_\_\_

HW#4 CVL851: Special Topics in Transportation, Spring 2023

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**Problem 4 (30 Points)**

1. Define measurable space, measure space, and probability space.
  2. Define random variable.
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