

Problem 1 (10 Points) Prove that Dirac measure is a measure. Prove if it is finite or σ -finite measure. Prove if it is complete or not.

Problem 2 (5 Points) Given a Hahn decomposition of a set X for a signed measure ν show the Jordan decomposition for the signed measure.

Problem 3 (10 Points) Prove that the union of a finite union of measurable sets is measurable.

Problem 4 (10 Points) Show the steps for constructing a measure for a set X . State the condition for on a set function defined on a collection S and the condition on S such that the collection S is measurable in the Caratheodory construction.